

Lösungen „Ableiten bis der Arzt kommt“ ohne Garantie :-)

a) $f'(x) = 2x - 20x^4$

b) $f'(x) = \frac{1}{2\sqrt{x}} - 1$

c) $f'(x) = \cos(x)\sqrt{x} + \frac{\sin(x)}{2\sqrt{x}}$

d) $f'(x) = -\frac{1}{x^2} + 2x$

$$f'(x) = -\frac{1}{x^2} \cos(x) - \frac{1}{x} \sin(x)$$

e) $f'(x) = \cos^2(x) - \sin^2(x)$

f) $f'(x) = 2 \sin(x) \cos(x)$

g) $f'(x) = 16x^3 - 36x^2 + 18x$

h) $f'(x) = 5(3x^3 - 2x^2)^4(9x^2 - 4x)$

i) $f'(x) = -3(\cos(x))^2 \sin(x)$

j) $f'(x) = -\frac{5}{2}x^{-\frac{3}{2}} = -\frac{5}{2\sqrt{x^3}}$

k) $f'(x) = -\frac{2}{x^3} + \frac{20}{x^5}$

l) $f'(x) = \frac{\frac{1}{2\sqrt{x}}(\sqrt{x}+3) - \frac{1}{2\sqrt{x}}(\sqrt{x}-3)}{(\sqrt{x}+3)^2} = \frac{\frac{6}{2\sqrt{x}}}{x+6\sqrt{x}+9}$

m) $f'(x) = \frac{2x - \cos(x) - x \sin(x) - \sin(x)}{(\cos(x) - x)^2}$

n) $f'(x) = \frac{\cos^2(x) + \sin^2(x)}{\cos^2(x)}$

o) $f'(x) = -\frac{1}{2\sqrt{\frac{1}{x}} \ln x^2}$

p) $f'(x) = \frac{x}{\sqrt{x^2-1}}$

q) $f'(x) = \frac{1}{2\sqrt{x+\sqrt{x}}} \ln\left(1 + \frac{1}{2\sqrt{x}}\right)$

r) $f'(x) = 3\left(\frac{x+2}{x}\right)^2 \ln\left(-\frac{2}{x^2}\right)$

s) $f'(x) = \cos\left(\frac{1}{x}\right) \ln\left(-\frac{1}{x^2}\right)$

t) $f'(x) = \sqrt{x^3+1} + \frac{3x^3}{2\sqrt{x^3+1}}$

u) $f'(x) = 4$

v) $f'(x) = -12 \ln(\cos(4x))^2 \ln(\sin(4x))$

w) $f'(x) = 6x + 12$

x) $f_t'(x) = \frac{tx+1-2t^2}{(tx+1)^3}$

y) $f_t'(x) = t^3 + 2t^2x + 3tx^2$

z) $f_t'(x) = 0$